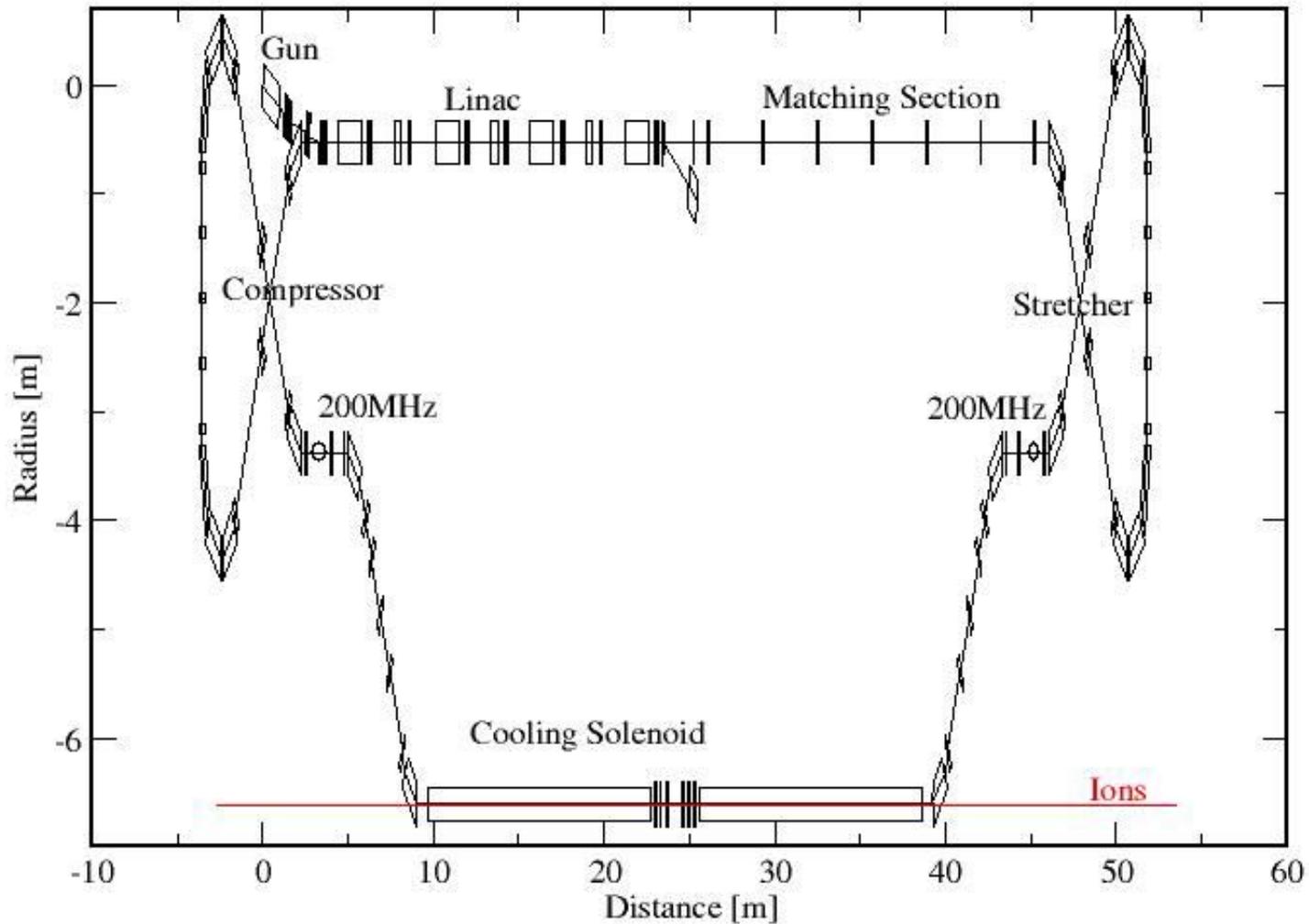
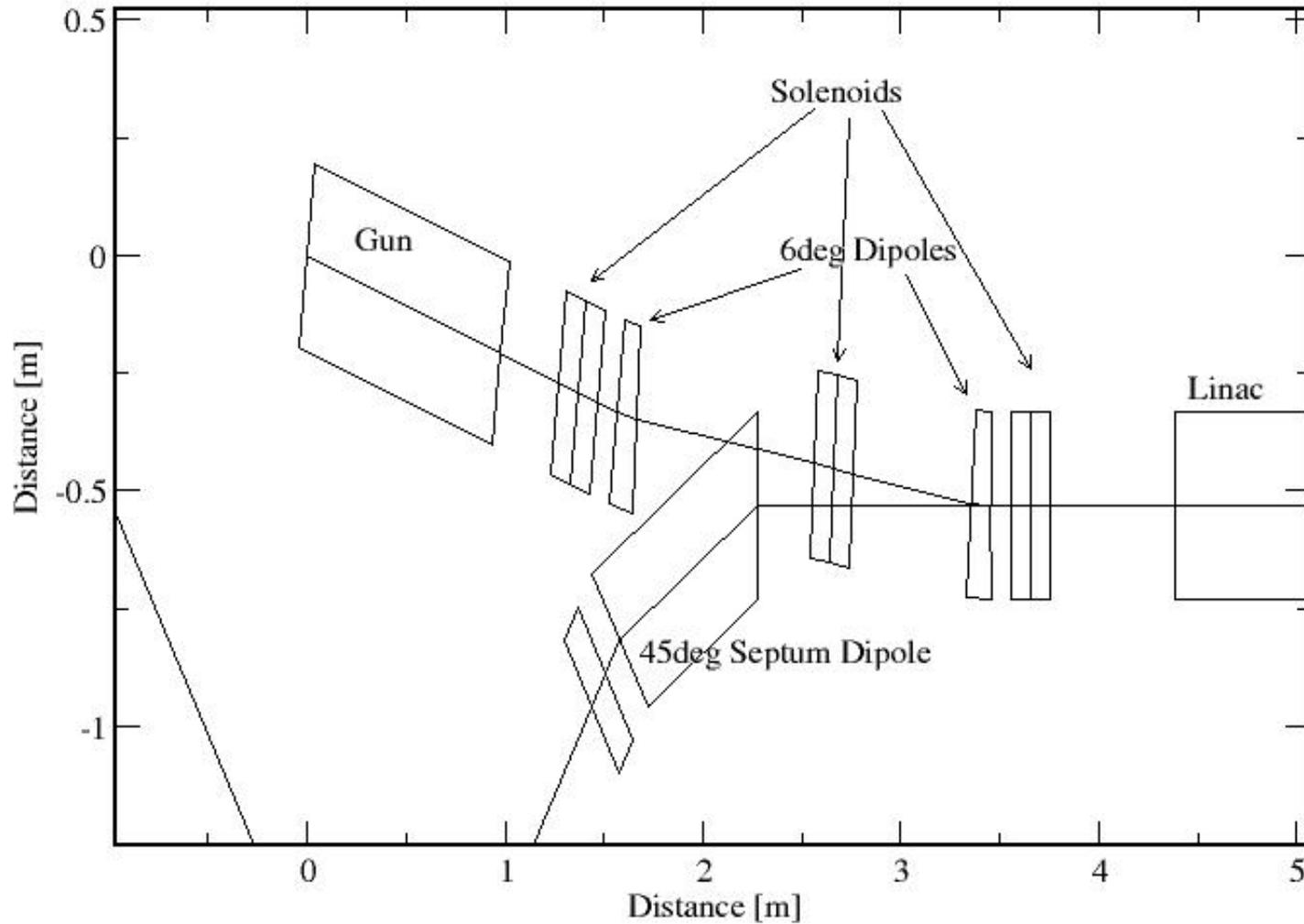

Beam Dynamics in the Electron Cooler

Jörg Kewisch

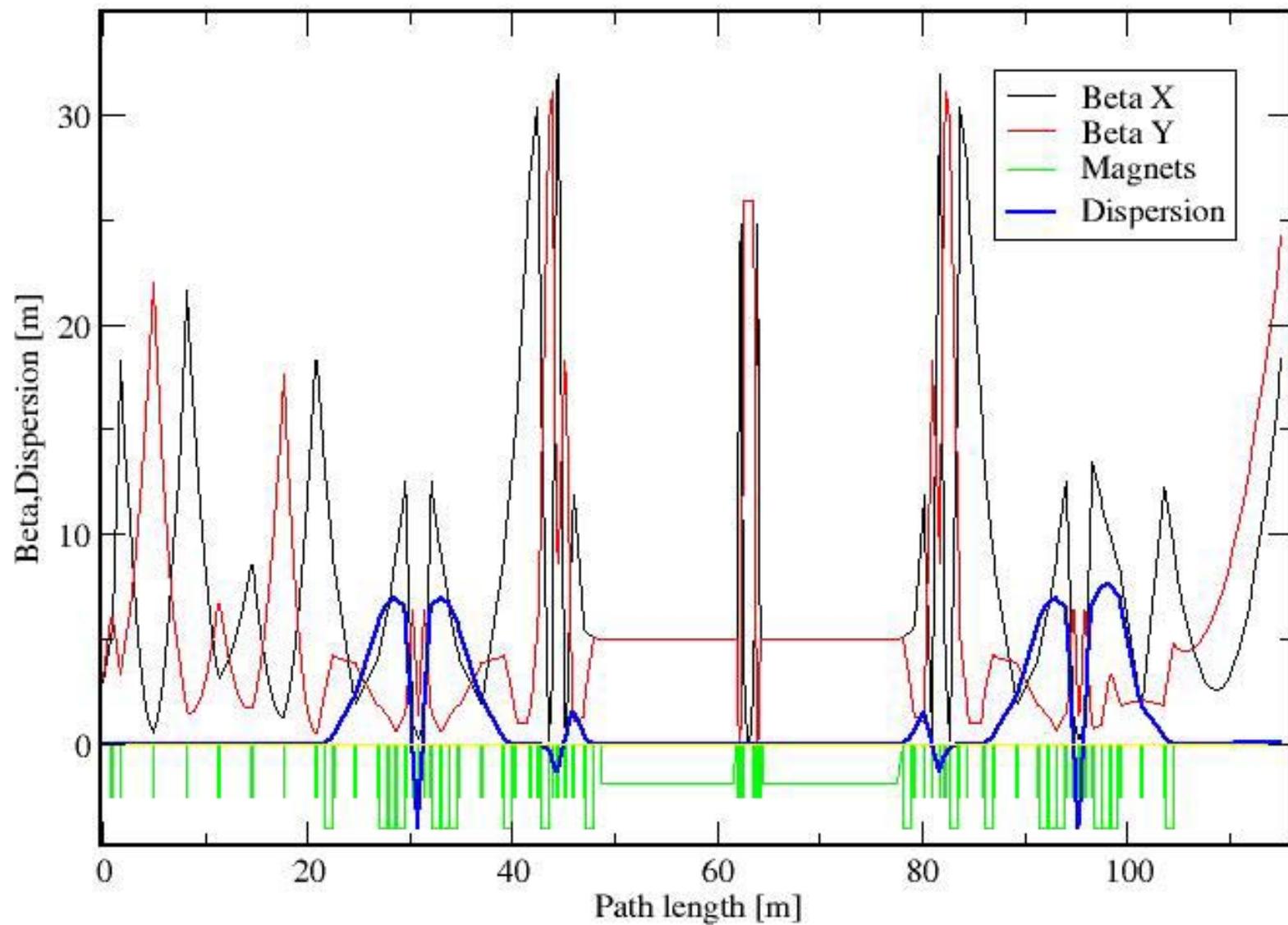
Cooler Layout



Cooler Layout



55 MeV Optics



Parameters

Cooling Section:

Energy: 55 MeV
Energy spread: $1 \cdot 10^{-4}$
Bunch length: 15 cm
Bunch radius: 1 mm
Emittance: 50 mm mrad
Solenoid: 1 Tesla

Linac:

700 MHz Cavities: 4
Gradient: 15 MV/m
2100 MHz Cavities: 3
Gradient: 7.5 MV/m
Power amplifiers: 50 kW

Arcs:

Max. Dispersion: 6 m
Max. Beam Size (rms): 5 cm
Stretch factor: 33 m

Gun:

Normal Conducting
700 MHz 2½ Cell
Bunch charge: 10 nC
Bunch frequency: 9.8 MHz
Beam Energy: 2.5 MeV
Power: 1 MW

What is a "Magnetized Beam", Bush's Theorem

When a non-magnetized beam enters a solenoid, the fringe field increases the normalized emittance:

$$\varepsilon_{inside}^2 = \varepsilon_{outside}^2 + R^2 \sigma^4 \gamma^2 \quad \text{with} \quad R = \frac{1}{2} \frac{e}{pc} B_s$$

A magnetized beam rotates around the longitudinal axis ($x \sim y'$, $y \sim -x'$), so that the effect of the fringe field is canceled.

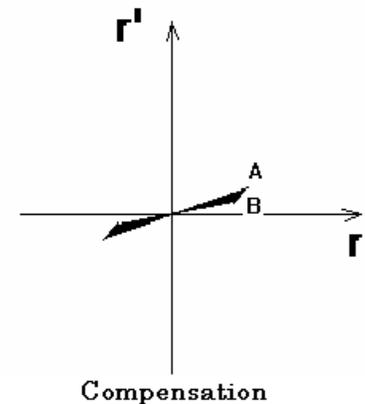
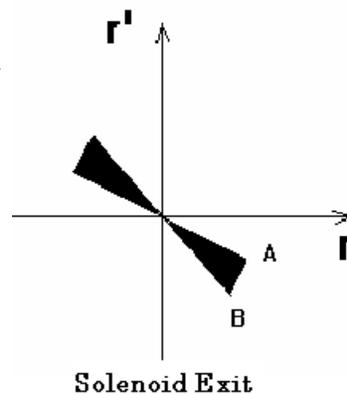
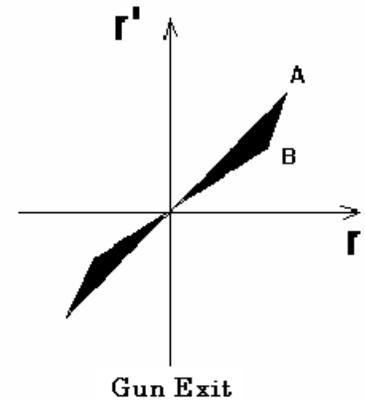
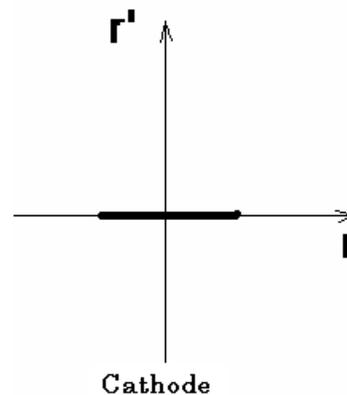
Busch's Theorem: If only axial symmetric fields are applied then:

$$r^2 \cdot \Theta' + r^2 \cdot \frac{e}{p} \cdot B = r_0^2 \cdot \frac{e}{p} \cdot B_0 \quad \text{with} \quad \Theta' = \left\langle \frac{y \cdot x' - x \cdot y'}{r^2} \right\rangle, p = m_e \gamma \beta c$$

- A magnetized beam can only be made using a magnetic field on the cathode!
- The beam transport matrix from the cathode to the cooling section must be axial symmetric.
- Non-linearities disturb the balance.

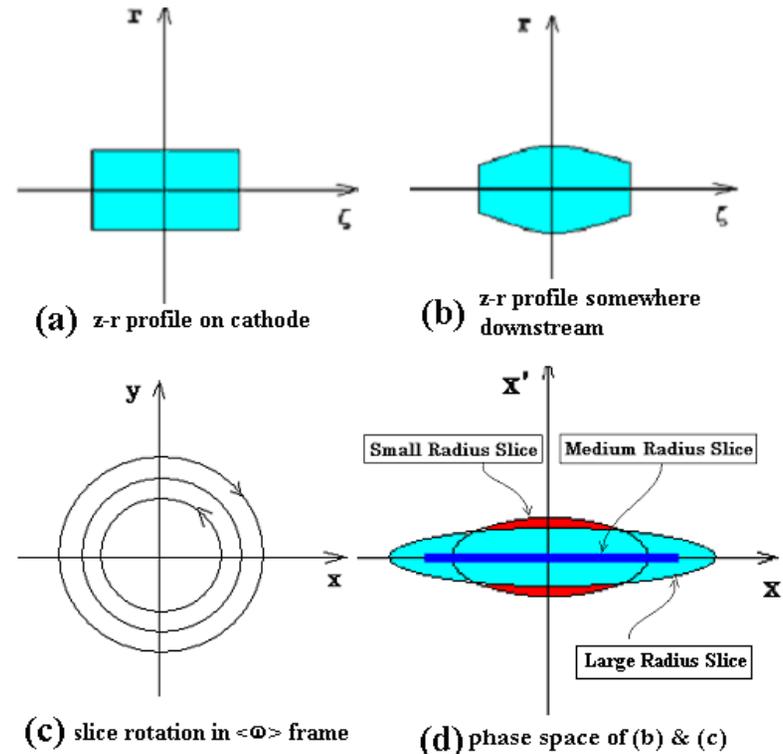
Traditional Emittance Compensation

- A bunch consists of longitudinal slices with small emittance.
- Slices experience different focusing from space charge and RF fields. The “over all” emittance increases.
- Focusing with a solenoid and subsequent space charge defocusing reverses this effect.
- After minimum emittance is obtained the bunch is accelerated, space charge is no longer important.



Magnetized Emittance Compensation

- For a magnetized beam a variation of radius causes strong emittance growth.
- Emittance compensation uses two focusing elements to keep radius and phase advance constant.
- The second focusing element is the fringe field of the accelerating cavity



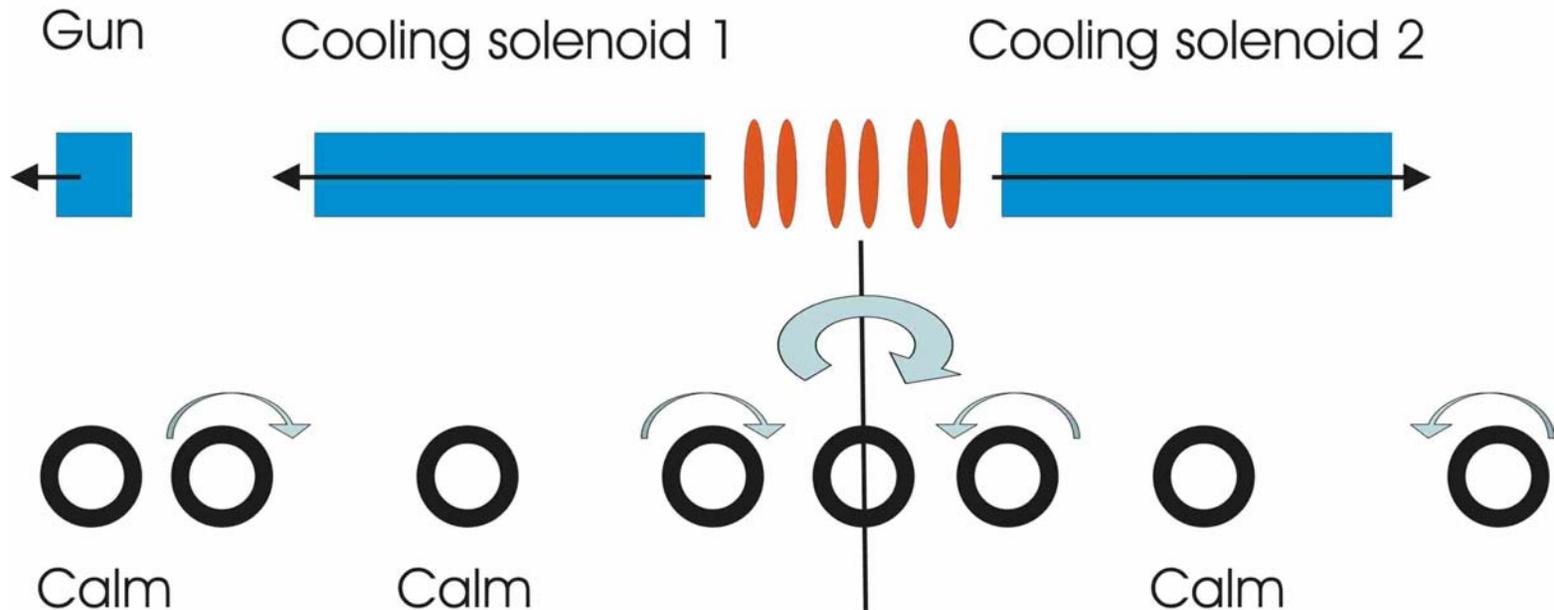
Stretcher/Compressor

- Energy spread reduced from $4 \cdot 10^{-4}$ to $1 \cdot 10^{-4}$ (rms)
- Energy spread $\frac{\Delta p}{p} = \pm 0.001$ introduced in the arc by mis-phasing last linac cavity.
- Arc provides $\Delta l = 33m \cdot \frac{\Delta p}{p}$, expands bunch length from 4.5 cm to 15 cm. Maximum dispersion is 6 m, maximum beam size 5 cm.
- 200 MHz normal conducting RHIC cavity used to remove energy spread.
- Second 200 MHz cavity introduces opposite energy spread
- Second arc shortens bunch length for energy recovery.

Solenoid Gap

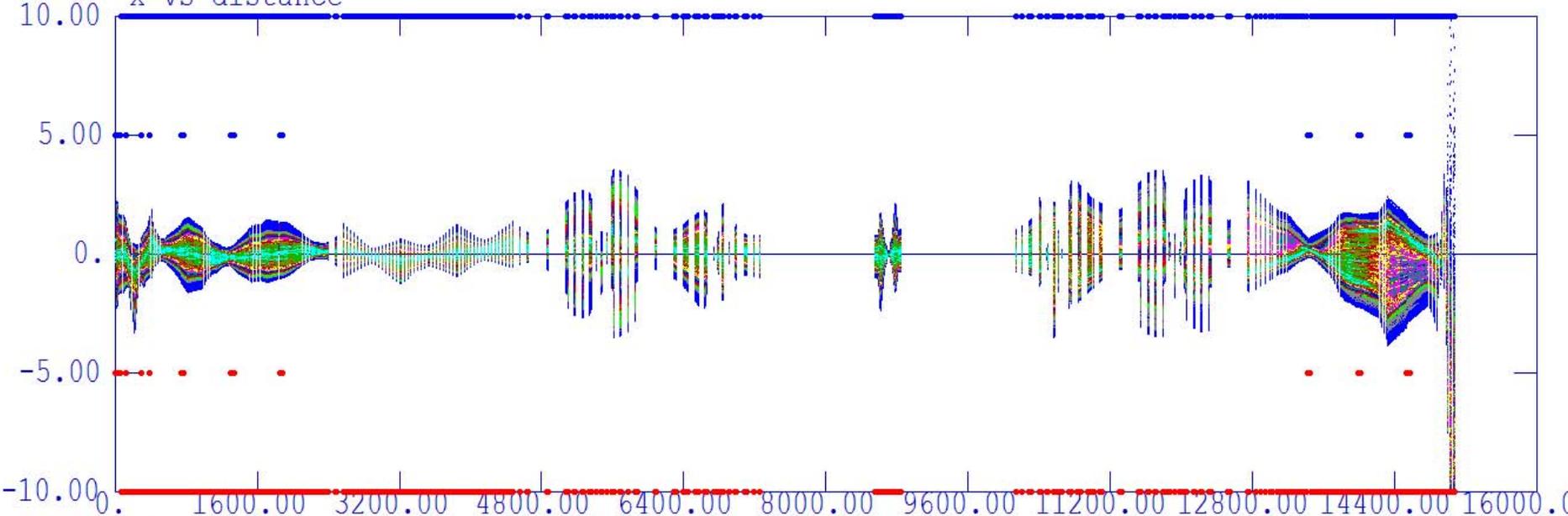
- For technical reasons the cooling solenoid will be split into two sections. Extra focusing is necessary to maintain magnetization.
- We will use quadrupoles to obtain $180^\circ/360^\circ$ phase advance. This allows opposing field direction in the solenoid halves.

Quad flip section

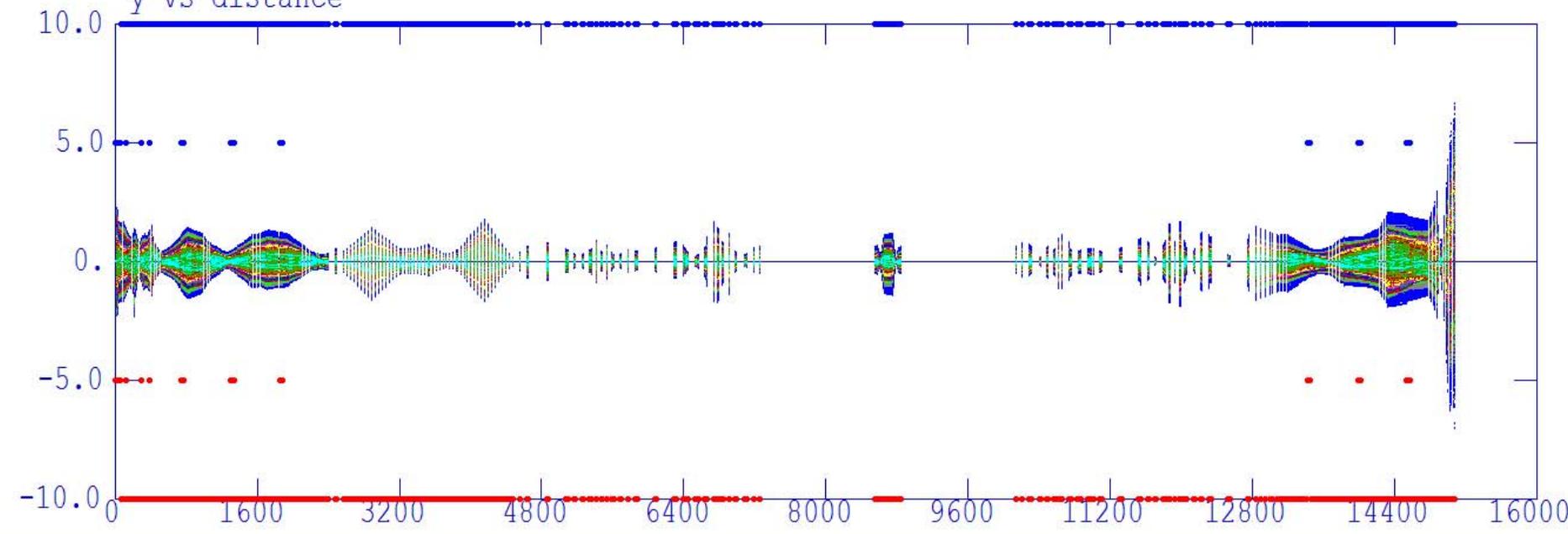


alpha=6, Mag.Cath.100G, Fld=9Mv/m, Charge=10nc, phs=30, R=15mm, FWHM=4deg, B1=2.1

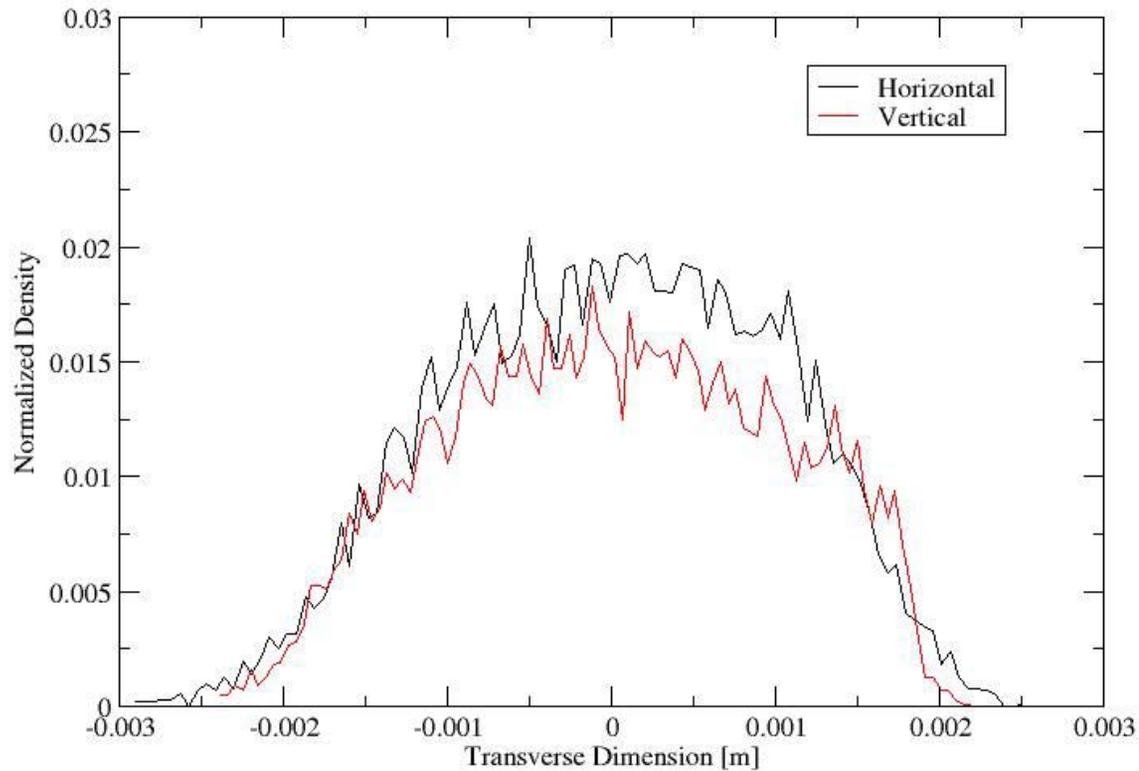
x vs distance



y vs distance



Profiles in the Cooler Solenoid

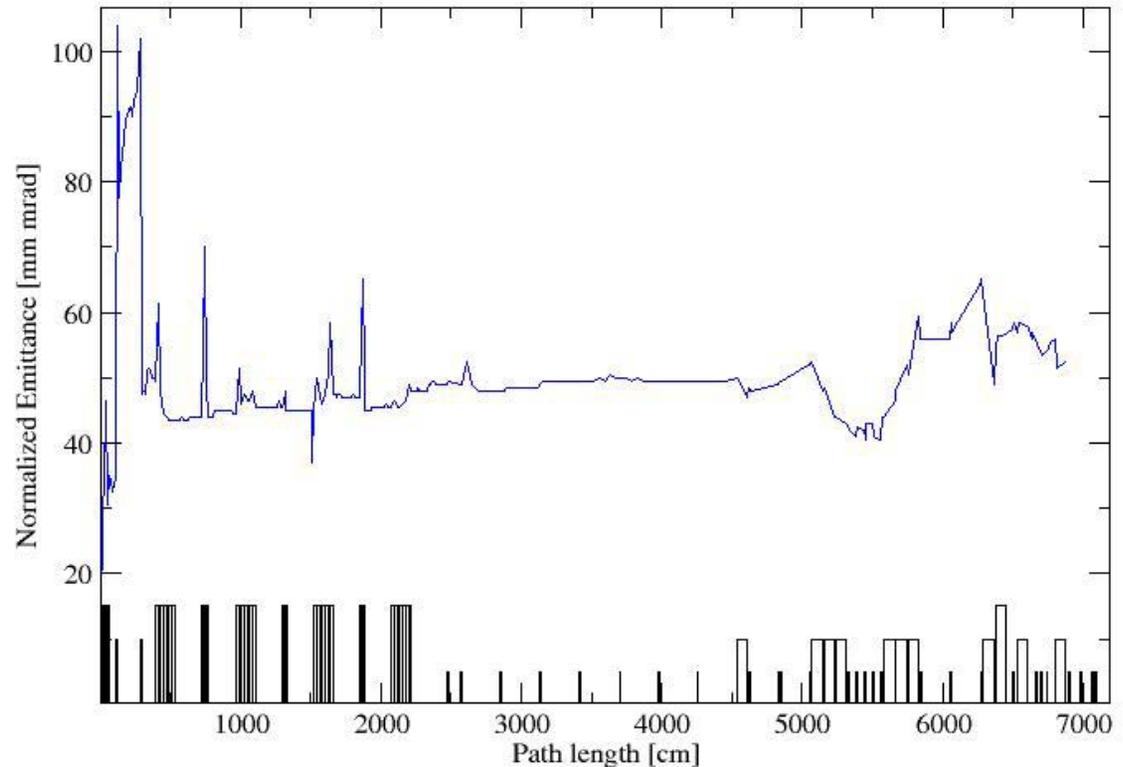


Front to End Simulation: Emittance

Method:

- Track electrons using PARMELA including space charge
- Apply linear transformation to make transport axial symmetric, remove dispersion
- Apply solenoid fringe field matrix
- Measure emittance

$$T_{\perp}[eV] = m_e c^2 \cdot \frac{\varepsilon_n^2}{\sigma^2} = 0.511 * (\varepsilon_n[mm \cdot mrad])^2$$



To Do

- **Tolerances: Alignment errors, non-linear field components.**
- **Instrumentation: Position, profile, energy, recombination.**
- **Correctors**
- **Commissioning plan.**
- **Further optimization of emittance.**
 - Focusing
 - “Constant Density Elliptical Shape” distribution
 - Bunching Cavity



Work in Progress